

Chain Rule:

example: $y = \sin(2x+3)$

s: $\sin(\quad)$ } $\cos(2x+3)$
c: $2x+3$ } 2

$$y' = 2 \cos(2x+3)$$

example: $y = (x^2+2x)^4$

s: $(\quad)^4$ } $4(x^2+2x)^3$
c: x^2+2x } $(2x+2)$

$$y' = 4(2x+2)(x^2+2x)^3$$

example: $y = \sqrt{3x^2-4} = (3x^2-4)^{\frac{1}{2}}$

s: $(\quad)^{\frac{1}{2}}$ } $\frac{1}{2}(3x^2-4)^{-\frac{1}{2}}$
c: $3x^2-4$ } $6x$

$$y' = 3x(3x^2-4)^{-\frac{1}{2}} = \frac{3x}{\sqrt{3x^2-4}}$$

example: $y = 2(x^2 - 3x + 4)^4$

s: $2()^4$ } $8(x^2 - 3x + 4)^3$
c: $x^2 - 3x + 4$ } $(2x - 3)$

$$y' = 8(2x - 3)(x^2 - 3x + 4)^3$$

Formula:

$$h = f(g(x))$$

s: $f()$ } $f'()$
c: $g(x)$ } $g'(x)$

$$h' = f'(g(x)) \cdot g'(x)$$

Peanuts:

example: $y = \sin^3(2x+3)$

$$y = [\sin(2x+3)]^3$$

S: $[\quad]^3$ } $\textcircled{3} [\sin(2x+3)]^2$
C: $\sin(2x+3)$ } $\cos(2x+3)$
P: $2x+3$ } $\textcircled{2}$

$$y' = 6 \cos(2x+3) \sin^2(2x+3)$$

example: $y = 3 \tan \sqrt{x+1}$

$$y = 3 \tan (x+1)^{1/2}$$

S: $3 \tan (\quad)$ } $3 \sec^2 ((x+1)^{1/2})$
C: $(x+1)^{1/2}$ } $\frac{1}{2} (x+1)^{-1/2}$
P: $x+1$ } 1

$$y' = \frac{\textcircled{3}}{2} (x+1)^{-1/2} \sec^2 (x+1)^{1/2}$$
$$= \frac{3 \sec^2(\sqrt{x+1})}{2\sqrt{x+1}}$$

$$y = -5 \cos^4(2x+3)$$

$$= -5 [\cos(2x+3)]^4$$

S: $-5 [\quad]^4$ } $\textcircled{-20} [\cos(2x+3)]^3$

C: $\textcircled{\cos(2x+3)}$ } $\textcircled{-2} \sin(2x+3)$

P: $\textcircled{2x+3}$ } $\textcircled{2}$

$$y' = \underline{\underline{40}} \sin(2x+3) \cos^3(2x+3)$$