

Average Rates of Change Problems

Name Key

Show all work leading to your answer. There will often be more than one way to solve the problem. You may use a calculator on * problems.

1. Suppose that the velocity function of a particle moving along a coordinate line is $v(t) = 3t^3 + 2$.

a) Find the average velocity over the time interval $1 \leq t \leq 4$.

$$\frac{1}{3} \int_1^4 v(t) dt = \frac{1}{3} \left(\frac{3t^4}{4} + 2t \Big|_1^4 \right) = \frac{1}{3} \left(3 \cdot 64 + 8 - \frac{3}{4} - 2 \right) = \frac{263}{4} \text{ or } 65.75$$

b) Find the average acceleration over the time interval $1 \leq t \leq 4$.

$$\frac{v(4) - v(1)}{4 - 1} = \frac{194 - 5}{3} = 63$$

2. Suppose that the acceleration function of a particle moving along a coordinate line is $a(t) = t + 1$. Find the average acceleration of the particle over the time interval $0 \leq t \leq 5$.

$$\frac{1}{5} \int_0^5 a(t) dt = \frac{1}{5} \left(\frac{t^2}{2} + t \Big|_0^5 \right) = \frac{1}{5} \left(\frac{25}{2} + 5 - 0 \right) = \frac{7}{2} \text{ or } 3.5$$

*3. During the first 40 seconds of a rocket flight, the rocket is propelled straight up so that in t seconds it reaches of height of $s(t) = \frac{t^3}{\sqrt{10}}$ feet.

a) What is the average height of the rocket during the first 40 seconds?

$$\frac{1}{40} \int_0^{40} s(t) dt = 5059.644 \text{ ft}$$

b) What is the average velocity of the rocket during the first 40 seconds?

$$v(t) = \frac{3}{\sqrt{10}} t^2$$
$$\frac{1}{40} \int_0^{40} v(t) dt = 505.964 \text{ ft/sec}$$

c) What is the average acceleration of the rocket during the first 40 seconds?

$$a(t) = \frac{6}{\sqrt{10}} t$$
$$\frac{1}{40} \int_0^{40} a(t) dt = 37.947 \text{ ft/sec}^2$$