AB Retest Practice Name _____ Applications of Differentiation 4.1-4.4, and f, f', f''

1. What are all values of x for which the function $f(x) = x^3 - 6x^2 + 9x - 1$ is decreasing?

2. Given the function $f(x) = x^4 + 2x^3$, find the relative extrema, and the points of inflection.

3. The figure shows the graph of the derivative of a function f. How many points of inflection does f have in the interval shown?



4. Let *f* be the function given by $f(x) = x^3 - 3x$. What are all values of *c* that satisfy the conclusion of the Mean Value Theorem on the closed interval [-1,2]?

5. What are all values of x for which the graph of $y = \frac{3}{3-x}$ is concave downward?

4. The function *f* is continuous for $-3 \le x \le 3$ and differentiable for $-3 \le x \le 3$. If f(-3) = 2 and f(3) = -4, which statement(s) must be true?

- I. There exists c, where -3 < c < 3, such that f'(c) = 0.
- II. There exists c, where -3 < c < 3, such that f'(c) = -1.
- III. There exists c, where $-3 \le c \le 3$, such that $f(c) \ge f(x)$ for all x on the closed interval $-3 \le c \le 3$.

5. Let $f''(x) = 4x^3 - 2x$ and let f(x) have critical numbers -1, 0, and 1. Use the Second Derivative Test to determine if any of the critical numbers gives a relative minimum.

6. The graph of f(x) is shown in the figure to the

right. Where is f' decreasing?



7. Where does the absolute maximum value of the function $f(x) = x^3 - 3x + 1$ occur on the interval [-3,2]?

8. Let f be a function that is continuous on the closed interval [0,3]. The function f and its derivatives have the properties indicated in the table below.

Х	0	0 <x<2< th=""><th>2</th><th>2<x<3< th=""><th>3</th><th>3<x<4< th=""><th>4</th></x<4<></th></x<3<></th></x<2<>	2	2 <x<3< th=""><th>3</th><th>3<x<4< th=""><th>4</th></x<4<></th></x<3<>	3	3 <x<4< th=""><th>4</th></x<4<>	4
f(x)	1	+	0	+	+1	+	-1
f'(x)	undefined	-	0	+	undefined	-	undefined
f''(x)	undefined	+	0	+	undefined	-	undefined

a) Find the x coordinate for each local extrema (identify whether it is a min or a max). Justify your answer.

b) Find the x- coordinate for any points of inflection. Justify your answer.

c) Where is f(x) concave down? Justify your answer.

d) Sketch the graph of a function with the given characteristics. Justify your answer.



9. For $y' = x^2(x+3)(x-2)$, find the x-values of any local max and min(Identify which are maximums and which are minimums).

10. $f(x) = \frac{2}{(x-1)^2}$ Does Rolle's Theorem Apply on the interval [0,2]?