Calculus Project - Volumes of Solids with Known Cross Section
Make a physical model of a solid with a known cross section on a base with a standard function. The following guidelines apply:


1) The base function(s) can be any non-linear function except a parabola, square root, or absolute value. (If using 2 functions, the 2 nd can be any of your choice).
2) The cross section can be any shape except a rectangle of constant height. If you choose a square or rectangle of changing height, your max grade will be a 90.
3) For the model, the materials can be no thicker than $0.5^{\prime \prime}$. Your model must be at least 6 inches long and have at least 12 cross sections.
4) Bonus points will be given for final shapes that look like a real-life object.

With your model, you must turn in the following:

1. A detailed graph of your base. You must partition your base into at least 12 partitions, with each partition being no more than a .5 inch wide. The partitions do not need to match the thickness of your actual building material.
2. Estimate the volume of your solid, using a Reimann Sum and your $\Delta x$. You can use a left, right, or midpoint Reimann Sum. Show all work in an organized manner.
3. Write and solve (by hand) a definite integral to find the exact volume of your solid. You must show all work that leads to your solution.

|  | Calculus Rubric: Volumes of Cross Section |  | names: |
| :---: | :---: | :---: | :---: |
|  |  | PROFICIENT | ADVANCED |
| Model | 40 | - Solid is mounted on a board(not poster board or butcher paper.\} (5) <br> - Material for cross sections are no more than . 5 " thick. (5) <br> - Solid is at least 6 inches long. (5) <br> - At least 12 cross sections are present on the model. (5) <br> - Model is neat and shows attention to detail. (5) <br> - Rubric is turned in with project with all group members names.(5) | In addition to PROFICIENT criteria ... <br> - Model depicts a character or object.(5) <br> - Model is exceptionally neat and well constructed.(5) |
|  |  | 0-----------------------------30 | 30---------- 40 |
| Content <br> Calculus <br> Information | 45 | - First base equation is nonlinear, and is not quadratic, square root, or absolute value. (5) <br> - Base is graphed neatly on graph paper with partitions shown.(5) <br> - All work for the estimation of the volume using a Reimann Sum is shown.(5) <br> - Integral and all work are shown clearly for the exact volume.(5) <br> - Answers are correct. (10) | In addition to PROFICIENT criteria ... <br> - Base equation(s) and cross sections are of a higher difficulty.(5) <br> - Work is typed using an equation editor.(5) <br> - Midpoint Sum is used instead of left or right.(5) |
|  |  | 0---------------------------30 | 30--------- 45 |
| Collaborative Work | 15 | These last 15 points will be a combination of teacher and partner input on how well your time is used, and how well you work as a team. |  |

## Grading Comments:

Calculus Project - Volumes of Revolution
Make a physical model of a Volume of Revolution about the $x$ or $y$-axis.


The following guidelines apply:

1) The function(s) can be any non-linear function except a parabola, square root, or absolute value. (If using 2 functions, the 2 nd can be any of your choice).
2) The materials can be no thicker than $0.5^{\prime \prime}$. Your model must be at least 6 inches long and have at least 12 circular cross sections.
3) Bonus points will be given for final shapes that look like a real-life object.

With your model, you must turn the following:

1. A detailed graph of the function you are rotating with boundaries marked. You will partition this shape into at least 12 partitions, with each partition being no more than a $1 / 2$ inch wide. The partitions do not need to match the thickness of your actual building material.
2. Estimate the volume of your solid, using a Reimann Sum and your $\Delta x$. You can use a left, right, or midpoint Reimann Sum. Show all work in an organized manner.
3. Write and solve (by hand) a definite integral to find the exact volume of your solid. You must show all work that leads to your solution.

|  | Calculus Rubric: Volumes of Rotation |  | names: |
| :---: | :---: | :---: | :---: |
|  |  | PROFICIENT | ADVANCED |
| Model | 40 | - Solid is constructed with a string. dowel, or wire through the center. (5) <br> - Material for cross sections are no more than . 5 " thick. (5) <br> - Solid is at least 6 inches long. (5) <br> - At least 12 cross sections are present on the model. (5) <br> - Model is neat and shows attention to detail. (5) <br> - Rubric is turned in with project with all group members names.(5) | In addition to PROFICIENT criteria ... <br> - Model depicts a character or object.(5) <br> - Model is exceptionally neat and well constructed.(5) |
|  |  | 0-----------------------------30 | 30----------40 |
| Content <br> Calculus <br> Information | 45 | - First equation is nonlinear, and is not quadratic, square root, or absolute value. (5) <br> - Function is graphed neatly on graph paper with partitions shown.(5) <br> - All work for the estimation of the volume using a Reimann Sum is shown.(5) <br> - Integral and all work are shown clearly for the exact volume.(5) <br> - Answers are correct. (10) | In addition to PROFICIENT criteria ... <br> - Equation(s) are of a higher difficulty.(5) <br> - Work is typed using an equation editor.(5) <br> - Midpoint Sum is used instead of left or right.(5) |
|  |  | 0---------------------------30 | 30---------- 45 |
| Collaborative Work | 15 | These last 15 points will be a combination of teacher and partner input on how well your time is used, and how well you work as a team. |  |

