AB Calculus (Calculator OK) Average vs. Instantaneous Rate of Change

1. Suppose $g(t) = 1 - t^2$ . a. Find the slope of the line secant to $g(t)$ from $t = -1$ to $t = 3$ .	d. If g(t) gives the temperature (°C) of a liquid at time t (sec), find the average rate of change of the temperature between t = 18 seconds and t = 21 seconds. Include units with your answer.
b. Find the average rate of change of g on the interval $[-1,5]$	
	f. Find the instantaneous rate of change of g at t = $-1$ .
c. Suppose g represents the position (in cm) of an object at time t seconds. Find the average velocity of the object on the time interval starting at t = -1 and lasting .1 seconds. Include units with your answer.	
	g. Find the slope of the line tangent to $g(t)$ at $t = 0$ . Then find the slope of the line normal(perpendicular) to the tangent line at $t = 0$ .
3. a)Use the limit definition to find the derivative of $f(x) = x^2 - 2x$	
b) Use the alternate form of the definition to find $f'(2)$ .	

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4. a) Use the limit definition to find the slope of the tangent line of g(x) = \frac{1}{x+2}.
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b) Use the alternate form of the definition to find g'(2).

5. The graph of the function k(x) is drawn below. Use it to answer the following questions.

- a. On what interval(s) is k(x) positive?
- b. On what interval(s) is k(x) < 0?
- c. On what interval(s) is k(x) increasing?
- d. On what interval(s) is k(x) decreasing?
- e. On what interval(s) does the line tangent to k(x) have a positive slope?
- g. On what interval(s) does the line tangent to k(x) have a negative slope?
- h. For which value(s) of x does the line tangent to k(x) have a slope of zero.

