

Name:

Stuff You Must Know Cold – Cal AB

Limits

Notation for:

Limit from the left of $f(x)$ as $x \rightarrow a$

Limit from the right of $f(x)$ as $x \rightarrow a$

$\lim_{x \rightarrow a} f(x)$ exists if :

=

Theorems:

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} =$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} =$$

Steps:

- 1.
- 2.
- 3.

Definition of Continuity:

A function is continuous at the point $x=a$ if and only if:

- 1.
- 2.
- 3.

Intermediate Value Theorem

Extreme Value Theorem

Rolle's Theorem

Derivatives

Definition of Derivative

$$\frac{d}{dx}(f(x)) =$$

Alternate Form of Def. of Derivative

$$\frac{d}{dx}(f(x)) \text{ at } x = a$$

Equation of a tangent line at $x=a$

Chain Rule

$f(g(x))$	
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Product Rule

$f \cdot g$	
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Quotient Rule

$\frac{f}{g}$	
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Curve Sketching and Analysis

Critical Points:

Increasing:

Decreasing:

Relative Min:

Relative Max:

Absolute Extrema:

Concave Up:

Concave Down:

Point of Inflection:

More Derivatives

Where u is a function of x and a is a constant

function	derivative
x^n	
$\sin u$	
$\cos u$	
$\tan u$	
$\csc u$	
$\sec u$	
$\cot u$	
$\arcsin u$	
$\arccos u$	
$\arctan u$	
$\operatorname{arccsc} u$	
$\operatorname{arcsec} u$	
$\operatorname{arccot} u$	
e^u	
$\ln u$	
a^u	
$\log_a u$	

Derivative of an Inverse

(a,b) on $f(x)$
 $g(x) = f^{-1}(x)$
 $g'(b) =$

The Mean Value Theorem (derivatives)

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The Fundamental Theorem of Calculus

$$\int_a^b f(x)dx =$$

$$F'(x) = f(x)$$

Corollary to FTC

$$\frac{d}{dx} \int_{h(x)}^{g(x)} f(t)dt =$$

Mean Value Theorem for Integrals

(Average Value)

Other integration rules:

$$\int x^n dx =$$

$$\int \tan u du =$$

$$\int \sec u du =$$

$$\int \csc u du =$$

$$\int \cot u du =$$

$$\int a^u du =$$

Area between two curves:

Solids of Revolution

Disk Method

Washer Method

Distance, Velocity, and Acceleration

$s(t)$ is the position function,

velocity =

acceleration =

speed =

Speed is increasing when

position =

Total distance

average velocity =

L'Hôpital's Rule :

Volumes of Known Cross Sections:

(Perpendicular to x-axis)

(Perpendicular to y-axis)

Squares:

Rectangles:

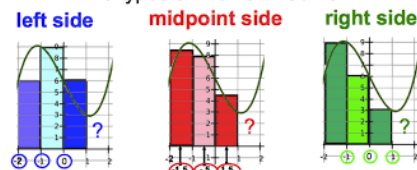
Equilateral Triangles:

Isosceles Right Triangles:

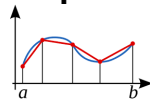
Semicircles:

Riemann Sums:

3 types of Riemann Sums



Trapezoidal Sum:



Area of a trapezoid:

$$\left(\frac{f(c_1) + f(c_2)}{2} \right) (\Delta x)$$

Limit definition of an Integral:

$$\text{Area} = \int_a^b f(x)dx =$$

Trig Study Sheet

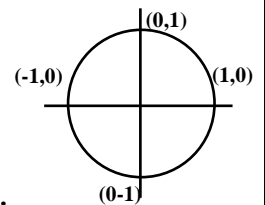
Signs: All Students Take Calculus

Values: sin, csc, tan, cot, cos, sec. All functions are positive.

	30°	45°	60°
sin θ			
cos θ			
tan θ			

Quadrants

(cos, sin)
tan = sin/cos



Trig Graphs:

$$y = \sin x$$

$$y = \cos x$$

$$y = \tan x$$

Pythagorean Identities:

• **Reciprocal Identities:**

• **Double Angles:**